## **Exercise**

### 2.1

1. Which of the following expressions are polynomials in one variable and which are not? State reasons for your answer.

(i) 
$$4x^2 - 3x + 7$$

Solution:

The equation  $4x^2 - 3x + 7$  can be written as  $4x^2 - 3x^1 + 7x^0$ 

Since x is the only variable in the given equation and the powers of x (i.e., 2, 1 and 0) are whole numbers, we can say that the expression  $4x^2 - 3x + 7$  is a polynomial in one variable.

(ii) 
$$y^2 + \sqrt{2}$$

Solution:

The equation  $y^2 + \sqrt{2}$  can be written as  $y^2 + \sqrt{2}$   $y^0$ 

Since y is the only variable in the given equation and the powers of y (i.e., 2 and 0) are whole numbers, we can say that the expression  $y^2 + \sqrt{2}$  is a polynomial in one variable.

(iii) 
$$3 \sqrt{t} + t \sqrt{2}$$

Solution:

The equation 3  $\sqrt{t}$  + t  $\sqrt{2}$  can be written as  $3t^{\frac{1}{2}} + \sqrt{2}t$ 

Though, t is the only variable in the given equation, the powers of t (i.e.,  $\frac{1}{2}$ ) is not a whole number. Hence, we can say that the expression 3  $\sqrt{t}$  + t  $\sqrt{2}$  is **not** a polynomial in one variable.

(iv) 
$$y + \frac{2}{y}$$

The equation  $y + \frac{2}{y}$  can be written as  $y+2y^{-1}$ Though, y is the only variable in the given equation, the powers of y (i.e.,-1) is not a whole number.

Hence, we can say that the expression  $y + \frac{2}{y}$  is **not** a polynomial in one variable.

(v) 
$$x^{10} + y^3 + t^{50}$$

Solution:

Here, in the equation  $x^{10} + y^3 + t^{50}$ 

Though, the powers, 10, 3, 50, are whole numbers, there are 3 variables used in the expression  $x^{10} + y^3 + t^{50}$ . Hence, it is **not** a polynomial in one variable.

## Exercise 2.1

#### 2. Write the coefficients of x2 in each of the following:

(i) 
$$2 + x^2 + x$$

Solution

The equation  $2 + x^2 + x$  can be written as  $2 + (1) x^2 + x$ 

We know that, coefficient is the number which multiplies the variable.

Here, the number that multiplies the variable x2 is 1

 $\therefore$ , the coefficients of  $x^2$  in  $2 + x^2 + x$  is 1.

#### (ii) $2 - x^2 + x^3$

Solution:

The equation  $2 - x^2 + x^3$  can be written as  $2 + (-1) x^2 + x^3$ 

We know that, coefficient is the number (along with its sign,i.e., - or +) which multiplies the variable.

Here, the number that multiplies the variable  $x^2$  is -1

 $\therefore$ , the coefficients of  $x^2$  in  $2 - x^2 + x^3$  is -1.

(iii) 
$$\frac{\pi}{2} x^2 + x$$

Solution:

The equation  $\frac{\pi}{2}$   $x^2 + x$  can be written as (  $\frac{\pi}{2}$  )  $x^2 + x$ 

We know that, coefficient is the number (along with its sign,i.e., - or +) which multiplies the variable.

Here, the number that multiplies the variable  $x^2$  is  $\frac{\pi}{2}$ 

$$\therefore$$
 , the coefficients of  $x^2$  in  $-\frac{\pi}{2}-x^2+x$  is  $-\frac{\pi}{2}$  .

(iv) 
$$\sqrt{2}$$
 x-1

Solution:

The equation  $\sqrt{2}$  x-1 can be written as  $0x^2 + \sqrt{2}$  x-1 [Since  $0x^2$  is 0]

We know that, coefficient is the number (along with its sign, i.e., - or +) which multiplies the variable.

Here, the number that multiplies the variable  $x^2$  is 0

 $\therefore$ , the coefficients of  $x^2$  in  $\sqrt{2}$  x-1 is 0.

## 3. Give one example each of a binomial of degree 35, and of a monomial of degree 100.

Binomial of degree 35: A polynomial having two terms and the highest degree 35 is called a binomial of degree 35

Eg., 3x35+5

Monomial of degree 100: A polynomial having one term and the highest degree 100 is called a monomial of degree 100

Eg., 4x100

#### Exercise 2.1

#### 4. Write the degree of each of the following polynomials:

(i)  $5x^3 + 4x^2 + 7x$ 

Solution:

The highest power of the variable in a polynomial is the degree of the polynomial.

Here,  $5x^3 + 4x^2 + 7x = 5x^3 + 4x^2 + 7x^1$ 

The powers of the variable x are: 3, 2, 1

 $\therefore$ , the degree of  $5x^3 + 4x^2 + 7x$  is 3 as 3 is the highest power of x in the equation.

#### (ii) $4-y^2$

Solution:

The highest power of the variable in a polynomial is the degree of the polynomial.

Here, in  $4 - y^2$ ,

The power of the variable y is: 2

 $\therefore$ , the degree of  $4 - y^2$  is 2 as 2 is the highest power of y in the equation.

#### (iii) $5t - \sqrt{7}$

Solution:

The highest power of the variable in a polynomial is the degree of the polynomial.

Here, in  $5t - \sqrt{7}$ ,

The power of the variable y is: 1

 $\therefore$ , the degree of 5t -  $\sqrt{7}$  is 1 as 1 is the highest power of y in the equation.

#### (iv) 3

Solution:

The highest power of the variable in a polynomial is the degree of the polynomial.

Here,  $3 = 3 \times 1 = 3 \times x^0$ 

The power of the variable here is: 0

: , the degree of 3 is 0.

#### 5. Classify the following as linear, quadratic and cubic polynomials:

Solution:

We know that,

Linear polynomial: A polynomial of degree one is called a linear polynomial.

Quadratic polynomial: A polynomial of degree two is called a quadratic polynomial.

Cubic polynomial: A polynomial of degree three a cubic polynomial.

(i) 
$$x^2 + x$$

Solution:

The highest power of  $x^2 + x$  is 2

..., the degree is 2

Hence,  $x^2 + x$  is a quadratic polynomial

### Exercise 2.1

(ii)  $x-x^3$ Solution: The highest power of  $x-x^3$  is 3  $\therefore$ , the degree is 3 Hence,  $x-x^3$  is a cubic polynomial

(iii)  $y + y^2 + 4$ Solution: The highest power of  $y + y^2 + 4$  is 2  $\therefore$ , the degree is 2 Hence,  $y + y^2 + 4$  is a quadratic polynomial

(iv) 1+x
Solution:
The highest power of 1 + x is 1
∴ , the degree is 1
Hence, 1 + x is a linear polynomial

(v) 3t
Solution:
The highest power of 3t is 1
∴ , the degree is 1
Hence, 3t is a linear polynomial

(vi) r²
Solution:
The highest power of r² is 2
∴ , the degree is 2
Hence, r² is a quadratic polynomial

(vii) 7x³

Solution:

The highest power of 7x³ is 3

∴, the degree is 3

Hence, 7x³ is a cubic polynomial

## Exercise 2.2

- 1. Find the value of the polynomial  $(x)=5x-4x^2+3$ x = 0(ii) x = -1(iii) x = 2Solution: Let  $f(x) = 5x-4x^2+3$ (i) When x=0 $f(0)=5(0)+4(0)^2+3$ =3 (ii) When x=-1 $f(x)=5x-4x^2+3$  $f(-1)=5(-1)-4(-1)^2+3$ =-5-4+3 =-6 (iii) When x=2  $f(x)=5x-4x^2+3$  $f(2)=5(2)-4(2)^2+3$
- 2. Find p(0), p(1) and p(2) for each of the following polynomials:
- (i)  $p(y)=y^2-y+1$ Solution:  $p(y)=y^2-y+1$   $\therefore p(0)=(0)^2-(0)+1=1$   $p(1)=(1)^2-(1)+1=1$  $p(2)=(2)^2-(2)+1=3$

=10-16+3 =-3

(ii)  $p(t)=2+t+2t^2 = t^3$ Solution:  $p(t)=2+t+2t^2-t^3$  $\therefore p(0)=2+0+2(0)^2-(0)^3=2$ 

 $p(1)=2+1+2(1)^2-(1)^3=2+1+2-1=4$  $p(2)=2+2+2(2)^2-(2)^3=2+2+8-8=4$ 

### (iii) $p(x)=x^3$ Solution: $p(x)=x^3$ $\therefore p(0)=(0)^3=0$ $p(1)=(1)^3=1$ $p(2)=(2)^3=8$

### Exercise 2.2

Page: 35
(iv)p(x)=(x-1)(x+1)
Solution:
$$p(x)=(x-1)(x+1)$$

$$\therefore p(0)=(0-1)(0+1)=(-1)(1)=-1$$

$$p(1)=(1-1)(1+1)=0(2)=0$$

$$p(2)=(2-1)(2+1)=1(3)=3$$

3. Verify whether the following are zeroes of the polynomial, indicated against them.

(i) 
$$p(x)=3x+1, x=-\frac{1}{3}$$
  
Solution:  
For,  $x=-\frac{1}{3}$ ,  $p(x)=3x+1$   
 $\therefore p(-\frac{1}{3})=3(-\frac{1}{3})+1=-1+1=0$   
 $\therefore -\frac{1}{3}$  is a zero of  $p(x)$ .

(ii) 
$$p(x)=5x-\pi, x=\frac{4}{5}$$

Solution:

For, 
$$x = \frac{4}{5}$$
  $p(x)=5x-\pi$   
 $\therefore p(\frac{4}{5})=5(\frac{4}{5})-\pi=4-\pi$   
 $\therefore \frac{4}{5}$  is not a zero of  $p(x)$ .

(iii) 
$$p(x)=x^2-1, x=1, -1$$
  
Solution:  
For,  $x=1, -1$ ;  
 $p(x)=x^2-1$ 

$$\therefore p(1)=1^{2}-1=$$

$$1-1=0$$

$$p(-1)=(-1)^{2}-1=1-1=0$$

$$\therefore 1, -1 \text{ are zeros of } p(x).$$
(iv)  $p(x)=(x+1)(x-2), x=-1, 2$ 
Solution:
For,  $x=-1,2$ ;
$$p(x)=(x+1)(x-2)$$

$$\therefore p(-1)=(-1+1)(-1-2)$$

$$=((0)(-3))=0$$

$$p(2)=(2+1)(2-2)=(3)(0)=0$$

$$\therefore -1, 2 \text{ are zeros of } p(x).$$
(v)  $p(x)=x^{2}, x=0$ 
Solution:

## Exercise 2.2

For, x=0  $p(x)=x^2$   $p(0)=0^2=0$  $\therefore 0$  is a zero of p(x).

(vi)p(x)=lx+m, x=- 
$$\frac{m}{l}$$

Solution:

For, 
$$x=-\frac{m}{l}$$
;  $p(x)=lx+m$   

$$\therefore p(-\frac{m}{l})=l(-\frac{m}{l})+m=-m+m=0$$

$$\therefore -\frac{m}{l}$$
 is a zero of  $p(x)$ .

(vii) 
$$p(x)=3x^2-1, x=-\frac{1}{\sqrt{3}}, \frac{2}{\sqrt{3}}$$

Solution:

For, 
$$x = -\frac{1}{\sqrt{3}}$$
,  $\frac{2}{\sqrt{3}}$ ;  $p(x) = 3x^2 - 1$   
 $\therefore p(-\frac{1}{\sqrt{3}}) = 3(-\frac{1}{\sqrt{3}})^2 - 1 = 3(\frac{1}{3}) - 1 = 1 - 1 = 0$   
 $\therefore p(\frac{2}{\sqrt{3}}) = 3(\frac{2}{\sqrt{3}})^2 - 1 = 3(\frac{4}{3}) - 1 = 4 - 1 = 3 \neq 0$   
 $\therefore -\frac{1}{\sqrt{3}}$  is a zero of  $p(x)$  but  $\frac{2}{\sqrt{3}}$  is not a zero of  $p(x)$ .

(viii) 
$$p(x)=2x+1, x=\frac{1}{2}$$
  
Solution:  
For,  $x=\frac{1}{2}$   $p(x)=2x+1$   
 $\therefore p(\frac{1}{2})=2(\frac{1}{2})+1=1+1=2\neq 0$ 

$$\therefore \frac{1}{2}$$
 is not a zero of p(x).

4. Find the zero of the polynomial in each of the following cases:

(i) 
$$p(x) = x + 5$$

Solution:

p(x)=x+5

⇒x+5=0

 $\Rightarrow x=-5$ 

:-5 is a zero polynomial of the polynomial p(x).

(ii) 
$$p(x) = x - 5$$

Solution:

p(x)=x-5

⇒x-5=0

#### Exercise 2.2

⇒x=5

 $\therefore$ 5 is a zero polynomial of the polynomial p(x).

(iii) 
$$p(x) = 2x + 5$$

Solution:

p(x)=2x+5

 $\Rightarrow 2x+5=0$ 

⇒2x=-4

⇒x=- - <del>[</del>

 $\therefore x = -\frac{5}{2}$  is a zero polynomial of the polynomial p(x).

(iv)p(x) = 3x - 2

Solution:

p(x)=3x-2

```
\Rightarrow3x-2=0
   \Rightarrow3x=2
               is a zero polynomial of the polynomial p(x).
(v) p(x) = 3x
Solution:
   p(x)=3x
    \Rightarrow 3x=0
   \Rightarrow x=0
   \therefore0 is a zero polynomial of the polynomial p(x).
(vi)p(x) = ax, a \neq 0
Solution:
   p(x)=ax
    \Rightarrowax=0
   \Rightarrow x=0
   x=0 is a zero polynomial of the polynomial p(x).
(vii)
            p(x) = cx + d, c \neq 0, c, d are real numbers.
Solution:
   p(x) = cx + d
   \Rightarrow cx + d =0
   \therefore x= \frac{-d}{c} is a zero polynomial of the polynomial p(x).
```

## Exercise 2.3

1. Find the remainder when x3+3x2+3x+1 is divided by

```
(i) x+1

Solution:

x+1=0

\Rightarrow x=-1

\thereforeRemainder:

p(-1)=(-1)^3+3(-1)^2+3(-1)+1

=-1+3-3+1

=0

(ii) x-\frac{1}{2}
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Solution:  $x - \frac{1}{2} = 0$   $\Rightarrow x = \frac{1}{2}$   $\therefore$ Remainder:  $p(\frac{1}{2}) = (\frac{1}{2})^3 + 3(\frac{1}{2})^2 + 3(\frac{1}{2}) + 1$   $= \frac{1}{8} + \frac{3}{4} + \frac{3}{2} + 1$  $= \frac{27}{8}$ 

(iii) x Solution: x=0  $\therefore$ Remainder:  $p(0)=(0)^3+3(0)^2+3(0)+1$ =1

(iv) x+ $\pi$ Solution: x+ $\pi$ =0 ⇒x= $-\pi$ ∴Remainder: p(0)=( $-\pi$ )<sup>3</sup>+3( $-\pi$ )<sup>2</sup>+3( $-\pi$ )+1 = $-\pi$ <sup>3</sup>+3 $\pi$ <sup>2</sup>-3 $\pi$ +1

(v) 5+2x Solution: 5+2x=0  $\Rightarrow 2x=-5$  $\Rightarrow x=-\frac{5}{2}$ 

## Exercise 2.3

∴Remainder:  $(-\frac{5}{2})^3+3(-\frac{5}{2})^2+3(-\frac{5}{2})+1=-\frac{125}{8}+\frac{75}{4}-\frac{15}{2}+1$   $=-\frac{27}{8}$ 

2. Find the remainder when  $x^3-ax^2+6x-a$  is divided by x-a.

Solution: Let  $p(x)=x^3-ax^2+6x-a$ x-a=0

∴x=a

Remainder:

$$p(a)= (a)^3 - a(a^2) + 6(a) - a$$
  
=  $a^3 - a^3 + 6a - a = 5a$ 

3. Check whether 7+3x is a factor of  $3x^3+7x$ .

Solution:

7+3x=0

⇒3x=-7 only if 7+3x divides  $3x^3+7x$  leaving no remainder. ⇒x=  $\frac{-7}{3}$ 

$$\Rightarrow_{X} = \frac{-7}{3}$$

∴Remainder:  

$$3(\frac{-7}{3})^3 + 7(\frac{-7}{3}) = -\frac{-343}{9} + \frac{-49}{3}$$

$$= \frac{-343 - |49|3}{9}$$

$$= \frac{-343 - 147}{9}$$

$$= \frac{-490}{9} \neq 0$$
∴7+3x is not a factor of  $3x^3 + 7x$ 

 $\therefore$ 7+3x is not a factor of 3x<sup>3</sup>+7x

- 1. Determine which of the following polynomials has (x + 1) a factor:
- (i)  $x^3+x^2+x+1$

```
Solution:
   Let p(x) = x^3 + x^2 + x + 1
   The zero of x+1 is -1. [x+1=0 \text{ means } x=-1]
   p(-1)=(-1)^3+(-1)^2+(-1)+1
            =-1+1-1+1
   ∴By factor theorem, x+1 is a factor of x^3+x^2+x+1
(ii) x^4 + x^3 + x^2 + x + 1
Solution:
   Let p(x) = x^4 + x^3 + x^2 + x + 1
   The zero of x+1 is -1. [x+1=0 \text{ means } x=-1]
   p(-1)=(-1)^4+(-1)^3+(-1)^2+(-1)+1
            =1-1+1-1+1
            =1 \neq 0
   :By factor theorem, x+1 is a factor of x^4 + x^3 + x^2 + x + 1
(iii)
            x^4 + 3x^3 + 3x^2 + x + 1
Solution:
    Let p(x) = x^4 + 3x^3 + 3x^2 + x + 1
    The zero of x+1 is -1.
    p(-1)=(-1)4+3(-1)3+3(-1)2+(-1)+1
            =1-3+3-1+1
            =1 \pm 0
    :By factor theorem, x+1 is a factor of x^4 + 3x^3 + 3x^2 + x + 1
(iv)x^3 - x^2 - (2 + \sqrt{2})x + \sqrt{2}
Solution:
   Let p(x) = x^3 - x^2 - (2 + \sqrt{2})x + \sqrt{2}
   The zero of x+1 is -1.
   \begin{array}{lll} p(-1) = & (-1)^3 - (-1)^2 - (2 + \sqrt{2})(-1) + \sqrt{2} \\ = & -1 - 1 + 2 + \sqrt{2} + \sqrt{2} \end{array}
            = 2 \sqrt{2}
   : By factor theorem, x+1 is not a factor of x^3 - x^2 - (2 + \sqrt{2})x + \sqrt{2}
```

- 2. Use the Factor Theorem to determine whether g(x) is a factor of p(x) in each of the following cases:
- (i)  $p(x)=2x^3+x^2-2x-1$ , g(x)=x+1

```
Solution:
   p(x)=2x^3+x^2-2x-1, g(x)=x+1
   g(x)=0
   \Rightarrow x+1=0
   \Rightarrow x=-1
   \thereforeZero of g(x) is -1.
   Now,
   p(-1)=2(-1)^3+(-1)^2-2(-1)-1
           =-2+1+2-1
   \thereforeBy factor theorem, g(x) is a factor of p(x).
(ii) p(x)=x^3+3x^2+3x+1, g(x)=x+2
Solution:
   p(x)=x3+3x2+3x+1, g(x)=x+2
   g(x)=0
   \Rightarrow x+2=0
   \Rightarrow x=-2
   \thereforeZero of g(x) is -2.
   Now,
   p(-2)=(-2)^3+3(-2)^2+3(-2)+1
           =-8+12-6+1
           =-1#0
   \thereforeBy factor theorem, g(x) is not a factor of p(x).
(iii)
           p(x)=x^3-4x^2+x+6, g(x)=x-3
Solution:
   p(x)=x^3-4x^2+x+6, g(x)=x-3
   g(x)=0
   \Rightarrow x-3=0
   ⇒x=3
   \thereforeZero of g(x) is 3.
   Now,
   p(3)=(3)^3-4(3)^2+(3)+6
           =27-36+3+6
   \thereforeBy factor theorem, g(x) is a factor of p(x).
```

- 3. Find the value of k, if x 1 is a factor of p(x) in each of the following cases:
- (i)  $p(x)=x^2+x+k$ Solution:

```
If x-1 is a
factor of p(x), then p(1)=0
        By Factor Theorem
        \Rightarrow (1)^2 + (1) + k = 0
        \Rightarrow1+1+k=0
        \Rightarrow2+k=0
        ⇒k=-2
     (ii) p(x)=2x^2+kx+\sqrt{2}
     Solution:
        If x-1 is a factor of p(x), then p(1)=0
         \Rightarrow 2(1)^2 + k(1) + \sqrt{2} = 0
        \Rightarrow2+k+ \sqrt{2} =0
        \Rightarrowk=-(2+ \sqrt{2})
                 p(x)=kx^2-\sqrt{2} x+1
     (iii)
     Solution:
        If x-1 is a factor of p(x), then p(1)=0
        By Factor Theorem
        \Rightarrow k(1)^2 - \sqrt{2} \quad (1)+1=0
\Rightarrow k = \sqrt{2} \quad -1
     (iv)p(x)=kx^2-3x+k
     Solution:
        If x-1 is a factor of p(x), then p(1)=0
        By Factor Theorem
        \Rightarrowk(1)<sup>2</sup>-3(1)+k=0
        \Rightarrowk-3+k=0
        ⇒2k-3=0
    4. Factorize:
     (i) 12x^2-7x+1
     Solution:
        Using the splitting the middle term method,
         We have to find a number whose sum=-7 and product=1 \times 12=12
         We get -3 and -4 as the numbers
                                                                        [-3+-4=-7 \text{ and } -3 \times -4=12]
```

### Exercise 2.4

 $12x^2-7x+1=12x^2-4x-3x+1$ 

$$=4x\ (3x-1)-1(3x-1)$$

$$=(4x-1)(3x-1)$$

$$=(4x-1)(3x-1)$$
(ii)  $2x^2+7x+3$ 
Solution:

Using the splitting the middle term method,
We have to find a number whose sum=7 and product= $2\times3=6$ 
We get 6 and 1 as the numbers
$$2x^2+7x+3=2x^2+6x+1x+3$$

$$=2x\ (x+3)+1(x+3)$$

$$=(2x+1)(x+3)$$
(iii)  $6x^2+5x-6$ 
Solution:
Using the splitting the middle term method,
We have to find a number whose sum=5 and product= $6\times-6=-36$ 
We get  $-4$  and  $9$  as the numbers
$$6x^2+5x-6=6x^2+9x-4x-6$$

$$=3x\ (2x+3)-2\ (2x+3)$$

$$=(2x+3)\ (3x-2)$$
(iv)  $3x^2-x-4$ 
Solution:
Using the splitting the middle term method,
We have to find a number whose sum= $-1$  and product= $3\times-4=-12$ 
We get  $-4$  and  $-4$  as the numbers
$$3x^2-x-4=3x^2-4x+3x-4$$

$$=3x^2-4x+3x-4$$

$$=3x^2-4x+3x-4$$

$$=3x^2-4x+3x-4$$

$$=(3x-4)+1(3x-4)$$

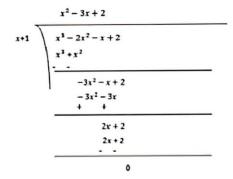
$$=(3x-4)(x+1)$$
5. Factorize:
(i)  $x^3-2x^2-x+2$ 
Factors of  $2$  are  $\pm 1$  and  $\pm 2$ 
By trial method, we find that  $p(1)=0$ 
So,  $(x+1)$  is factor of  $p(x)$ 

## **Exercise**

### 2.4

Now,  $p(x)=x^3-2x^2-x+2$   $p(-1)=(-1)^3-2(-1)^2-(-1)+2$  =-1-1+1+2=0

Therefore, (x+1) is the factor of p(x)



Now, Dividend = Divisor × Quotient + Remainder

$$\begin{array}{c} (x+1)(x^2-3x+2) = & (x+1)(x^2-x-2x+2) \\ = & (x+1)(x(x-1)-2(x-1)) \\ = & (x+1)(x-1)(x+2) \end{array}$$

#### (ii) $x^3-3x^2-9x-5$

Solution:

Let  $p(x) = x^3 - 3x^2 - 9x - 5$ 

Factors of 5 are ±1 and ±5

By trial method, we find that

p(5) = 0

So, (x-5) is factor of p(x)

Now,

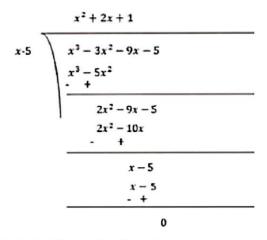
$$p(x) = x^3-3x^2-9x-5$$

$$p(5) = (5)^3-3(5)^2-9(5)-5$$

$$= 125-75-45-5$$

Therefore, (x-5) is the factor of p(x)

## Exercise 2.4



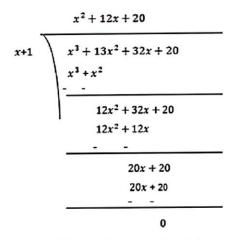
Now, Dividend = Divisor × Quotient + Remainder

$$\begin{array}{l} (x-5)(x^2+2x+1) = & (x-5)(x^2+x+x+1) \\ = & (x-5)(x(x+1)+1(x+1)) \\ = & (x-5)(x+1)(x+1) \end{array}$$

(iii) 
$$x^3+13x^2+32x+20$$
  
Solution:  
Let  $p(x) = x^3+13x^2+32x+20$   
Factors of 20 are  $\pm 1$ ,  $\pm 2$ ,  $\pm 4$ ,  $\pm 5$ ,  $\pm 10$  and  $\pm 20$   
By trial method, we find that  $p(-1) = 0$   
So,  $(x+1)$  is factor of  $p(x)$   
Now,  
 $p(x) = x^3+13x^2+32x+20$   
 $p(-1) = (-1)^3+13(-1)^2+32(-1)+20$   
 $= -1+13-32+20$   
 $= 0$ 

Therefore, (x+1) is the factor of p(x)

## Exercise 2.4



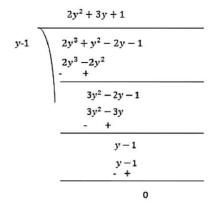
Now, Dividend = Divisor × Quotient + Remainder

$$(x+1)(x^2+12x+20) = (x+1)(x^2+2x+10x+20) = (x-5)x(x+2)+10(x+2) = (x-5)(x+2)(x+10)$$

(iv) 
$$2y^3+y^2-2y-1$$
  
Solution:  
Let  $p(y) = 2y^3+y^2-2y-1$   
Factors  $= 2 \times (-1) = -2$  are  $\pm 1$  and  $\pm 2$   
By trial method, we find that  $p(1) = 0$   
So,  $(y-1)$  is factor of  $p(y)$   
Now,  
 $p(y) = 2y^3+y^2-2y-1$   
 $p(1) = 2(1)^3+(1)^2-2(1)-1$   
 $= 2+1-2$ 

Therefore, (y-1) is the factor of p(y)

## Exercise 2.4



Now, Dividend ≈ Divisor × Quotient + Remainder

$$\begin{array}{l} (y-1)(2y^2+3y+1) = & (y-1)(2y^2+2y+y+1) \\ = & (y-1)(2y(y+1)+1(y+1)) \\ = & (y-1)(2y+1)(y+1) \end{array}$$

### Exercise 2.5

#### 1. Use suitable identities to find the following products:

(i) 
$$(x + 4) (x + 10)$$

Solution:

Using the identity, 
$$(x + a) (x + b) = x^2 + (a + b)x + ab$$
  
[Here, a=4 and b=10]  
We get,

$$(x+4)(x+10) = x^2 + (4+10)x + (4\times10)$$
  
=  $x^2 + 14x + 40$ 

(ii) 
$$(x + 8) (x - 10)$$

Solution:

Using the identity, 
$$(x + a) (x + b) = x^2 + (a + b)x + ab$$
  
[Here, a=8 and b=-10]  
We get,  
 $(x+8)(x-10)=x^2+(8+(-10))x+(8\times(-10))$   
 $=x^2+(8-10)x-80$   
 $=x^2-2x-80$ 

(iii) 
$$(3x+4)(3x-5)$$

Solution:

Using the identity, 
$$(x + a) (x + b) = x^2 + (a + b)x + ab$$
  
[Here,  $x=3x$ ,  $a=4$  and  $b=-5$ ]  
We get,  
 $(3x+4)(3x-5)=(3x)^2+4+(-5)3x+4\times(-5)$ 

$$(3x+4)(3x-5)=(3x)^2+4+(-5)3x+4\times(-5)$$

$$=9x^2+3x(4-5)-20$$

$$=9x^2-3x-20$$

(iv)(
$$y^2 + \frac{3}{2}$$
)( $y^2 - \frac{3}{2}$ )

Using the identity, 
$$(x + y) (x - y) = x^2 - y^2$$
  
[Here,  $x=y^2$  and  $y=\frac{3}{2}$ ]

We get,

$$(y^2 + \frac{3}{2})(y^2 - \frac{3}{2})$$
 =  $(y^2)^2 - (\frac{3}{2})^2$   
=  $y^4 - \frac{9}{4}$ 

```
2. Evaluate the following products without multiplying directly:
   (i) 103 × 107
   Solution:
      103×107=(100+3)×(100+7)
Exercise 2.5
      Using identity, [(x+a)(x+b)=x2+(a+b)x+ab]
      Here, x=100
             a=3
             b=7
      We get, 103×107=(100+3)×(100+7)
                      =(100)^2+(3+7)100+(3\times7)
                      =10000+1000+21
                      =11021
   (ii) 95 \times 96
   Solution:
      95×96=(100-5)×(100-4)
      Using identity, [(x-a)(x-b)=x^2+(a+b)x+ab
      Here, x=100
             a=-5
             b=-4
      We get, 95×96=(100-5)×(100-4)
                    =(100)^2+100(-5+(-4))+(-5\times-4)
                    =10000-900+20
                    =9120
   (iii)
             104 \times 96
   Solution:
    104×96=(100+4)×(100-4)
   Using identity, [(a+b)(a-b)=a^2-b^2]
   Here,
              a=100
             b=4
   We get, 104×96=(100+4)×(100-4)
                    =(100)^2-(4)^2
                    =10000-16
```

3. Factorize the following using appropriate identities:

=9984

#### (i) $9x^2+6xy+y^2$

Solution:

 $9x^2+6xy+y^2=(3x)^2+(2\times 3x\times y)+y^2$ Using identity,  $x^2+2xy+y^2=(x+y)^2$ Here, x=3xy=y

#### Exercise 2.5

$$9x^{2}+6xy+y^{2}=(3x)^{2}+(2\times 3x\times y)+y^{2}$$

$$=(3x+y)^{2}$$

$$=(3x+y)(3x+y)$$

#### (ii) $4y^2-4y+1$

Solution:

$$\begin{array}{l} 4y^2 - 4y + 1 = (2y)^2 - (2 \times 2y \times 1) + 12 \\ \text{Using identity, } x^2 - 2xy + y^2 = (x - y)^2 \\ \text{Here, } x = 2y \\ y = 1 \\ 4y^2 - 4y + 1 = (2y)^2 - (2 \times 2y \times 1) + 1^2 \\ = (2y - 1)^2 \\ = (2y - 1)(2y - 1) \end{array}$$

(iii) 
$$x^2 - \frac{y^2}{100}$$

Solution:

$$x^{2} - \frac{y^{2}}{100} = x^{2} - (\frac{y}{10})^{2}$$
  
Using identity,  $x^{2} - y^{2} = (x - y)(x y)$   
Here,  $x = x$   
 $y = \frac{y}{10}$ 

$$x^2 - \frac{y^2}{100} \approx x^2 - (\frac{y}{10})^2$$
  
= $(x - \frac{y}{10})(x + \frac{y}{10})$ 

4. Expand each of the following, using suitable identities:

(i) 
$$(x+2y+4z)^2$$
  
(ii)  $(2x-y+z)^2$   
(iii)  $(-2x+3y+2z)^2$   
(iv)  $(3a-7b-c)^2$   
(v)  $(-2x+5y-3z)^2$   
(vi)  $(\frac{1}{4} a-\frac{1}{2} b+1)^2$ 

Solutions:

6) 
$$(x+2y+4z)^2$$
  
Solution:  
Using identity,  $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$   
Here,  $x=x$   
 $y=2y$   
 $z=4z$   
 $(x+2y+4z)^2 = x^2+(2y)^2+(4z)^2+(2\times x\times 2y)+(2\times 2y\times 4z)+(2\times 4z\times x)$   
 $=x^2+4y^2+16z^2+4xy+16yz+8xz$   
(ii)  $(2x-y+z)^2$   
Solution:  
Using identity,  $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$   
Here,  $x=2x$   
 $y=-y$   
 $z=z$   
 $(2x-y+z)^2 = (2x)^2+(-y)^2+z^2+(2\times 2x\times -y)+(2\times -y\times z)+(2\times z\times 2x)$   
 $=4x^2+y^2+z^2-4xy-2yz+4xz$   
(iii)  $(-2x+3y+2z)^2$   
Solution:  
Using identity,  $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$   
Here,  $x=-2x$   
 $y=3y$   
 $z=2z$ 

$$(-2x+3y+2z)^{2}$$

$$=(-2x)^{2}+(3y)^{2}+(2z)^{2}+(2x-2x\times3y)+(2\times3y\times2z)+(2\times2z\times-2x)$$

$$=4x^{2}+9y^{2}+4z^{2}-12xy+12yz-8xz$$
(iv)  $(3a-7b-c)^{2}$ 
Solution:
Using identity,  $(x+y+z)^{2}=x^{2}+y^{2}+z^{2}+2xy+2yz+2zx$ 
Here,  $x=3a$ 

$$y=-7b$$

$$z=-c$$

$$(3a-7b-c)^{2}=(3a)^{2}+(-7b)^{2}+(-c)^{2}+(2\times3a\times-7b)+(2\times-7b\times-c)+(2\times-c\times3a)$$

$$=9a^{2}+49b^{2}+c^{2}-42ab+14bc-6ca$$

(v) 
$$(-2x + 5y - 3z)^2$$
  
Solution:  
Using identity,  $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$   
Here,  $x = -2x$   
 $y = 5y$   
 $z = -3z$   
 $(-2x+5y-3z)^2 = (-2x)^2 + (5y)^2 + (-3z)^2 + (2x-2x \times 5y) + (2x \times 5y \times -3z) + (2x-3z \times -2x)$   
 $= 4x^2 + 25y^2 + 9z^2 - 20xy - 30yz + 12zx$ 

(vi) 
$$(\frac{1}{4} \ a - \frac{1}{2} \ b+1)^2$$
  
Solution:  
Using identity,  $(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$   
Here,  $x = \frac{1}{4} \ a$   
 $y = -\frac{1}{2} \ b$   
 $z = 1$   
 $(\frac{1}{4} \ a - \frac{1}{2} \ b+1)^2 = (\frac{1}{4} \ a)^2 + (-\frac{1}{2} \ b)^2 + (1)^2 + (2 \times \frac{1}{4} \ a \times -\frac{1}{2} \ b) + (2 \times -\frac{1}{2} \ b \times 1) + (2 \times 1 \times 1) + (2 \times$ 

$$= \frac{1}{16} a^{2} + \frac{1}{4} b^{2} + 1^{2} - \frac{2}{8} ab - \frac{2}{2} b + \frac{2}{4} a$$

$$= \frac{1}{16} a^{2} + \frac{1}{4} b^{2} + 1 - \frac{1}{4} ab - b + \frac{1}{2} a$$

#### 5. Factorize:

(i) 
$$4x^2+9y^2+16z^2+12xy-24yz-16xz$$

(ii) 
$$2x^2+y^2+8z^2-2 \sqrt{2} xy+4 \sqrt{2} yz-8xz$$

Solutions:

(i) 
$$4x^2+9y^2+16z^2+12xy-24yz-16xz$$

Solution:

Using identity, 
$$(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$$

We can say that, 
$$x^2 + y^2 + z^2 + 2xy + 2yz + 2zx = (x + y + z)^2$$

$$4x^{2}+9y^{2}+16z^{2}+12xy-24yz-16xz = (2x)^{2}+(3y)^{2}+(-4z)^{2}+(2\times2x\times3y)+(2\times3y\times-4z)+(2\times-4z\times2x)$$

$$=(2x+3y-4z)^{2}$$

$$=(2x+3y-4z)(2x+3y-4z)$$

#### Exercise 2.5

(ii) 
$$2x^2+y^2+8z^2-2 \sqrt{2} xy+4 \sqrt{2} yz-8xz$$

Solution:

Using identity, 
$$(x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$$

We can say that, 
$$x^2 + y^2 + z^2 + 2xy + 2yz + 2zx = (x + y + z)^2$$

$$2x^2+y^2+8z^2-2 \sqrt{2} xy+4 \sqrt{2} yz-8xz$$

$$= (-\sqrt{2} \times x)^2 + (y)^2 + (2 \times \sqrt{2} \times z)^2 + (2 \times - \sqrt{2} \times x \times y) + (2 \times y \times 2)^2 + (2 \times y \times$$

#### 6. Write the following cubes in expanded form:

- (i)  $(2x+1)^3$
- (ii)  $(2a-3b)^3$

(iii) 
$$(\frac{3}{2}x+1)^3$$

$$(iv)(x-\frac{2}{3}y)^3$$

Solutions:

(i) 
$$(2x+1)^3$$
  
Solution:  
Using identity,  $(x + y)^3 = x^3 + y^3 + 3xy (x + y)$   
 $(2x+1)^3 = (2x)^3 + 1^3 + (3 \times 2x \times 1)(2x+1)$   
 $= 8x^3 + 1 + 6x(2x+1)$   
 $= 8x^3 + 12x^2 + 6x + 1$   
(ii)  $(2a-3b)^3$   
Solution:  
Using identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$   
 $(2a-3b)^3 = (2a)^3 - (3b)^3 - (3 \times 2a \times 3b)(2a-3b)$   
 $= 8a^3 - 27b^3 - 18ab(2a-3b)$ 

 $=8a^3-27b^3-36a^2b+54ab^2$ 

(iii) 
$$(\frac{3}{2}x+1)^3$$

Solution:

Using identity, 
$$(x + y)^3 = x^3 + y^3 + 3xy (x + y)$$
  
 $(\frac{3}{2} + x^{2})^3 = (\frac{3}{2} + x)^3 + 1^3 + (3 \times \frac{3}{2} + x^{2})(\frac{3}{2} + x^{2})$   
 $= \frac{27}{8} + x^3 + 1 + \frac{9}{2} + x(\frac{3}{2} + x^{2})$   
 $= \frac{27}{8} + x^3 + 1 + \frac{27}{4} + x^2 + \frac{9}{2} + x$   
 $= \frac{27}{8} + x^3 + \frac{27}{4} + x^2 + \frac{9}{2} + x + 1$ 

(iv) 
$$(x - \frac{2}{3} y)^3$$
  
Solution:  
Using identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$   
 $(x - \frac{2}{3} y)^3 = (x)^3 - (\frac{2}{3} y)^3 - (3 \times x \times \frac{2}{3} y)(x - \frac{2}{3} y)$   
 $= (x)^3 - \frac{8}{27} y^3 - 2xy(x - \frac{2}{3} y)$   
 $= (x)^3 - \frac{8}{27} y^3 - 2x^2y + \frac{4}{3} xy^2$ 

- 7. Evaluate the following using suitable identities:
- (i)  $(99)^3$
- (ii)  $(102)^3$

```
(iii)
           (998)^3
Solutions:
(i) (99)^3
Solution:
    We can write 99 as 100-1
   Using identity, (x-y)^3 = x^3 - y^3 - 3xy(x-y)
                     (99)^3 = (100-1)^3
                           =(100)^3-1^3-(3\times100\times1)(100-1)
                           =1000000-1-300(100-1)
                           = 1000000 - 1 - 30000 + 300
                           =970299
(ii) (102)^3
Solution:
    We can write 102 as 100+2
   Using identity, (x + y)^3 = x^3 + y^3 + 3xy(x + y)
                 (100+2)^3 = (100)^3 + 2^3 + (3 \times 100 \times 2)(100+2)
                           = 1000000 + 8 + 600(100 + 2)
                           = 1000000 + 8 + 60000 + 1200
                           = 1061208
(iii)
           (998)^3
Solution:
    We can write 99 as 1000-2
   Using identity, (x - y)^3 = x^3 - y^3 - 3xy(x - y)
                   (998)^3 = (1000-2)^3
                           =(1000)^3-2^3-(3\times1000\times2)(1000-2)
                           = 1000000000 - 8 - 6000(1000 - 2)
                           = 1000000000 - 8 - 6000000 + 12000
                           =994011992
```

### Exercise 2.5

- 8. Factorise each of the following:
- (i)  $8a^3+b^3+12a^2b+6ab^2$
- (ii) 8a3-b3-12a2b+6ab2
- (iii)  $27 125a^3 135a + 225a^2$
- $(iv)64a^3-27b^3-144a^2b+108ab^2$

(v) 
$$27p^3 - \frac{1}{216} - \frac{9}{2}p^2 + \frac{1}{4}p$$

Solutions:

(i)  $8a^3+b^3+12a^2b+6ab^2$ 

Solution:

```
The expression,
8a^3+b^3+12a^2b+6ab^2 can be written as (2a)^3+b^3+3(2a)^2b+3(2a)(b)^2
    8a^3+b^3+12a^2b+6ab^2 = (2a)^3+b^3+3(2a)^2b+3(2a)(b)^2
                            =(2a+b)^3
                            =(2a+b)(2a+b)(2a+b)
    Here, the identity, (x + y)^3 = x^3 + y^3 + 3xy(x + y) is used.
(ii) 8a^3-b^3=12a^2b+6ab^2
Solution:
The expression, 8a^3-b^3-12a^2b+6ab^2 can be written as (2a)^3-b^3-3(2a)^2b+3(2a)(b)^2
    8a^3-b^3-12a^2b+6ab^2
                          =(2a)^3-b^3-3(2a)^2b+3(2a)(b)^2
                            =(2a-b)^3
                            =(2a-b)(2a-b)(2a-b)
   Here, the identity, (x - y)^3 = x^3 - y^3 - 3xy(x - y) is used.
            27 - 125a^3 - 135a + 225a^2
(iii)
Solution:
The expression, 27 - 125a^3 - 135a + 225a^2 can be written as 3^3 - (5a)^3 - 3(3)^2(5a) + 3(3)(5a)^2
    27 - 125a^3 - 135a + 225a^2 = 3^3 - (5a)^3 - 3(3)^2(5a) + 3(3)(5a)^2
                            =(3-5a)^3
                            =(3-5a)(3-5a)(3-5a)
    Here, the identity, (x - y)^3 = x^3 - y^3 - 3xy(x - y) is used.
(iv)64a3-27b3-144a2b+108ab2
Solution:
The expression, 64a^3-27b^3-144a^2b+108ab^2 can be written as (4a)^3-(3b)^3-3(4a)^2(3b)+3(4a)(3b)^2
    64a^3-27b^3-144a^2b+108ab^2=(4a)^3-(3b)^3-3(4a)^2(3b)+3(4a)(3b)^2
                            =(4a-3b)^3
                            =(4a-3b)(4a-3b)(4a-3b)
```

#### Exercise 2.5

(v) 
$$27p^3 - \frac{1}{216} - \frac{9}{2} p^2 + \frac{1}{4} p$$
  
Solution:  
The expression,  $27p^3 - \frac{1}{216} - \frac{9}{2} p^2 + \frac{1}{4} p$  can be written as  $(3p)^3 - (\frac{1}{6})^3 - 3(3p)^2 (\frac{1}{6})^3 + 3(3p)(\frac{1}{6})^2$ 

Here, the identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$  is used.

- 9. Verify:
- (i)  $x^3+y^3=(x+y)(x^2-xy+y^2)$ (ii)  $x^3-y^3=(x-y)(x^2+xy+y^2)$

Solutions:

- (i)  $x^3+y^3=(x+y)(x^2-xy+y^2)$ We know that,  $(x+y)^3 = x^3+y^3+3xy(x+y)$   $\Rightarrow x^3+y^3=(x+y)^3-3xy(x+y)$   $\Rightarrow x^3+y^3=(x+y)[(x+y)^2-3xy]$ Taking(x+y) common  $\Rightarrow x^3+y^3=(x+y)[(x^2+y^2+2xy)-3xy]$  $\Rightarrow x^3+y^3=(x+y)(x^2+y^2-xy)$
- (ii)  $x^3-y^3=(x-y)(x^2+xy+y^2)$ We know that, $(x-y)^3 = x^3-y^3-3xy(x-y)$   $\Rightarrow x^3-y^3=(x-y)^3+3xy(x-y)$   $\Rightarrow x^3-y^3=(x-y)[(x-y)^2+3xy]$ Taking(x+y) common $\Rightarrow x^3-y^3=(x-y)[(x^2+y^2-2xy)+3xy]$  $\Rightarrow x^3+y^3=(x-y)(x^2+y^2+xy)$
- 10. Factorize each of the following:
- (i)  $27y^3+125z^3$
- (ii) 64m3-343n3

Solutions:

(i)  $27y^3+125z^3$ 

The expression,  $27y^3+125z^3$  can be written as  $(3y)^3+(5z)^3$   $27y^3+125z^3 = (3y)^3+(5z)^3$ We know that,  $x^3+y^3=(x+y)(x^2-xy+y^2)$   $\therefore 27y^3+125z^3 = (3y)^3+(5z)^3$   $=(3y+5z)[(3y)^2-(3y)(5z)+(5z)^2]$  $=(3y+5z)(9y^2-15yz+25z^2)$ 

(ii) 64m<sup>3</sup>-343n<sup>3</sup>

The expression,  $64\text{m}^3$ – $343\text{n}^3$  can be written as  $(4\text{m})^3$ – $(7\text{n})^3$   $64\text{m}^3$ – $343\text{n}^3$  = $(4\text{m})^3$ – $(7\text{n})^3$ We know that,  $x^3$ – $y^3$ =(x– $y)(x^2$ +xy+ $y^2)$ 

Exercise 2.5

 $\therefore$  64m<sup>3</sup>-343n<sup>3</sup> =(4m)<sup>3</sup>-(7n)<sup>3</sup>

=
$$(4m+7n)[(4m)^2+(4m)(7n)+(7n)^2]$$
  
= $(4m+7n)(16m^2+28mn+49n^2)$ 

#### 11. Factorise : $27x^3+y^3+z^3-9xyz$

Solution:

The expression 
$$27x^3+y^3+z^3-9xyz$$
 can be written as  $(3x)^3+y^3+z^3-3(3x)(y)(z)$   
 $27x^3+y^3+z^3-9xyz$  = $(3x)^3+y^3+z^3-3(3x)(y)(z)$ 

We know that, 
$$x^3 + y^3 + z^3 - 3xyz = (x + y + z)(x^2 + y^2 + z^2 - xy - yz - zx)$$

$$\begin{array}{l} \therefore \ \ 27x^3 + y^3 + z^3 - 9xyz = (3x)^3 + y^3 + z^3 - 3(3x)(y)(z) \\ = (3x + y + z)(3x)^2 + y^2 + z^2 - 3xy - yz - 3xz \\ = (3x + y + z)(9x^2 + y^2 + z^2 - 3xy - yz - 3xz) \end{array}$$

#### 12. Verify that:

$$x^3+y^3+z^3-3xyz=\frac{1}{2}(x+y+z)[(x-y)^2+(y-z)^2+(z-x)^2]$$

Solution:

We know that,

$$x^{3}+y^{3}+z^{3}-3xyz = (x+y+z)(x^{2}+y^{2}+z^{2}-xy-yz-xz)$$

$$\Rightarrow x^{3}+y^{3}+z^{3}-3xyz = \frac{1}{2} \times (x+y+z)[2(x^{2}+y^{2}+z^{2}-xy-yz-xz)]$$

$$= \frac{1}{2} (x+y+z)(2x^{2}+2y^{2}+2z^{2}-2xy-2yz-2xz)$$

$$= \frac{1}{2} (x+y+z)[(x^{2}+y^{2}-2xy)+(y^{2}+z^{2}-2yz)+(x^{2}+z^{2}-2xz)]$$

$$= \frac{1}{2} (x+y+z)[(x-y)^{2}+(y-z)^{2}+(z-x)^{2}]$$

#### 13. If x + y + z = 0, show that $x^3 + y^3 + z^3 = 3xyz$ .

Solution:

We know that,

$$x^{3}+y^{3}+z^{3}=3xyz = (x + y + z)(x^{2} + y^{2} + z^{2} - xy - yz - xz)$$
  
Now, according to the question, let  $(x + y + z) = 0$ ,  
then,  $x^{3}+y^{3}+z^{3}=3xyz = (0)(x^{2}+y^{2}+z^{2}-xy-yz-xz)$   
 $\Rightarrow x^{3}+y^{3}+z^{3}-3xyz = 0$   
 $\Rightarrow x^{3}+y^{3}+z^{3} = 3xyz$ 

Hence Proved

#### 14. Without actually calculating the cubes, find the value of each of the following:

(i) 
$$(-12)^3+(7)^3+(5)^3$$

(ii) (28)<sup>3</sup>+(-15)<sup>3</sup>+ (-13)<sup>3</sup>

## Exercise 2.5

(i) 
$$(-12)^3+(7)^3+(5)^3$$

Solution:

$$(-12)^3+(7)^3+(5)^3$$

Let 
$$a=-12$$

b=7

c=5

We know that if x + y + z = 0, then  $x^3+y^3+z^3=3xyz$ .

Here, -12+7+5=0

$$\therefore (-12)^3 + (7)^3 + (5)^3 = 3xyz$$
$$= 3 \times -12 \times 7 \times 5$$

$$= -1260$$

(ii)  $(28)^3 + (-15)^3 + (-13)^3$ 

Solution:

$$(28)^3 + (-15)^3 + (-13)^3$$

$$b = -15$$

$$c = -13$$

We know that if x + y + z = 0, then  $x^3+y^3+z^3=3xyz$ .

Here, 
$$x + y + z = 28 - 15 - 13 = 0$$

$$\therefore (28)^3 + (-15)^3 + (-13)^3 = 3xyz$$
= 0+3(28)(-15)(-13)
= 16380

15. Give possible expressions for the length and breadth of each of the following rectangles, in which their areas are given:

(i) Area: 25a<sup>2</sup>-35a+12

(ii) Area:  $35y^2+13y-12$ 

Solution:

(i) Area: 25a2-35a+12

Using the splitting the middle term method, We have to find a number whose sum= -35 and product= $25 \times 12=300$  We get -15 and -20 as the numbers [-15+-20=-35 and -3  $\times$  -4=300]

#### Exercise 2.5

```
25a^{2}-35a+12 = 25a^{2}-15a-20a+12
= 5a(5a-3)-4(5a-3)
= (5a-4)(5a-3)
Possible expression for length = 5a-4
Possible expression for breadth = 5a-3
```

(ii) Area:  $35y^2+13y-12$ Using the s<sub>1</sub> "" e term method, We have to soe sum= 13 and product=35 × -1 12=420 We get -15 and 28 as the numbers [-15+28=-35 and -15 × 28 = 420]  $35y^2+13y-12 = 35y^2-15y+28y-12 = 5y(7y-3)+4(7y-3)$ 

= (5y+4)(7y-3)Possible expression for length
Possible expression for breadth = (5y+4) = (7y-3)

# 16. What are the possible expressions for the dimensions of the cuboids whose volumes are given below?

(i) Volume: 3x<sup>2</sup>-12x (ii) Volume: 12ky<sup>2</sup>+8ky-20k

#### Solution:

(i) Volume:  $3x^2-12x$ 

 $3x^2-12x$  can be written as 3x(x-4) by taking 3x out of both the terms.

Possible expression for length = 3 Possible expression for breadth = xPossible expression for height = (x-4)

(ii) Volume: 12ky2+8ky-20k

 $12ky^2+8ky-20k$  can be written as  $4k(3y^2+2y-5)$  by taking 4k out of both the terms.  $12ky^2+8ky-20k=4k(3y^2+2y-5)$ 

[Here,  $3y^2+2y-5$  can be written as  $3y^2+5y-3y-5$  using splitting the middle term method.] = $4k(3y^2+5y-3y-5)$ 

=4k[y(3y+5)-1(3y+5)]=4k(3y+5)(y-1)

Possible expression for length = 4kPossible expression for breadth = (3y + 5)Possible expression for height = (y - 1)